



National  
Qualifications  
2017

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**X757/77/11**

**Physics  
Relationships Sheet**

WEDNESDAY, 17 MAY

9:00 AM – 11:30 AM

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## Relationships required for Physics Advanced Higher

$$v = \frac{ds}{dt}$$

$$a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

$$\omega = \frac{d\theta}{dt}$$

$$\alpha = \frac{d\omega}{dt} = \frac{d^2\theta}{dt^2}$$

$$\omega = \omega_o + \alpha t$$

$$\theta = \omega_o t + \frac{1}{2}\alpha t^2$$

$$\omega^2 = \omega_o^2 + 2\alpha\theta$$

$$s = r\theta$$

$$v = r\omega$$

$$a_t = r\alpha$$

$$a_r = \frac{v^2}{r} = r\omega^2$$

$$F = \frac{mv^2}{r} = mr\omega^2$$

$$T = Fr$$

$$T = I\alpha$$

$$L = mvr = mr^2\omega$$

$$L = I\omega$$

$$E_k = \frac{1}{2}I\omega^2$$

$$F = G\frac{Mm}{r^2}$$

$$V = -\frac{GM}{r}$$

$$v = \sqrt{\frac{2GM}{r}}$$

apparent brightness,  $b = \frac{L}{4\pi r^2}$

Power per unit area =  $\sigma T^4$

$$L = 4\pi r^2\sigma T^4$$

$$r_{\text{Schwarzschild}} = \frac{2GM}{c^2}$$

$$E = hf$$

$$\lambda = \frac{h}{p}$$

$$mvr = \frac{nh}{2\pi}$$

$$\Delta x \Delta p_x \geq \frac{h}{4\pi}$$

$$\Delta E \Delta t \geq \frac{h}{4\pi}$$

$$F = qvB$$

$$\omega = 2\pi f$$

$$a = \frac{d^2y}{dt^2} = -\omega^2 y$$

$$y = A \cos \omega t \quad \text{or} \quad y = A \sin \omega t$$

$$v = \pm \omega \sqrt{(A^2 - y^2)}$$

$$E_K = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$E_P = \frac{1}{2} m \omega^2 y^2$$

$$y = A \sin 2\pi \left( ft - \frac{x}{\lambda} \right)$$

$$E = kA^2$$

$$\phi = \frac{2\pi x}{\lambda}$$

$$\text{optical path difference} = m\lambda \quad \text{or} \quad \left( m + \frac{1}{2} \right) \lambda$$

where  $m = 0, 1, 2, \dots$

$$\Delta x = \frac{\lambda l}{2d}$$

$$d = \frac{\lambda}{4n}$$

$$\Delta x = \frac{\lambda D}{d}$$

$$n = \tan i_p$$

$$F = \frac{Q_1 Q_2}{4\pi \epsilon_0 r^2}$$

$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

$$V = \frac{Q}{4\pi \epsilon_0 r}$$

$$F = QE$$

$$V = Ed$$

$$F = IlB \sin \theta$$

$$B = \frac{\mu_0 I}{2\pi r}$$

$$c = \frac{1}{\sqrt{\epsilon_0 \mu_0}}$$

$$t = RC$$

$$X_C = \frac{V}{I}$$

$$X_C = \frac{1}{2\pi fC}$$

$$\mathcal{E} = -L \frac{dI}{dt}$$

$$E = \frac{1}{2} LI^2$$

$$X_L = \frac{V}{I}$$

$$X_L = 2\pi fL$$

$$\frac{\Delta W}{W} = \sqrt{\left( \frac{\Delta X}{X} \right)^2 + \left( \frac{\Delta Y}{Y} \right)^2 + \left( \frac{\Delta Z}{Z} \right)^2}$$

$$\Delta W = \sqrt{\Delta X^2 + \Delta Y^2 + \Delta Z^2}$$

$$d = \bar{v}t$$

$$s = \bar{v}t$$

$$v = u + at$$

$$s = ut + \frac{1}{2}at^2$$

$$v^2 = u^2 + 2as$$

$$s = \frac{1}{2}(u+v)t$$

$$W = mg$$

$$F = ma$$

$$E_w = Fd$$

$$E_p = mgh$$

$$E_k = \frac{1}{2}mv^2$$

$$P = \frac{E}{t}$$

$$p = mv$$

$$Ft = mv - mu$$

$$F = G \frac{Mm}{r^2}$$

$$t' = \frac{t}{\sqrt{1 - (v/c)^2}}$$

$$l' = l\sqrt{1 - (v/c)^2}$$

$$f_o = f_s \left( \frac{v}{v \pm v_s} \right)$$

$$z = \frac{\lambda_{\text{observed}} - \lambda_{\text{rest}}}{\lambda_{\text{rest}}}$$

$$z = \frac{v}{c}$$

$$v = H_0 d$$

$$W = QV$$

$$E = mc^2$$

$$E = hf$$

$$E_k = hf - hf_0$$

$$E_2 - E_1 = hf$$

$$T = \frac{1}{f}$$

$$v = f\lambda$$

$$d \sin \theta = m\lambda$$

$$n = \frac{\sin \theta_1}{\sin \theta_2}$$

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{\lambda_1}{\lambda_2} = \frac{v_1}{v_2}$$

$$\sin \theta_c = \frac{1}{n}$$

$$I = \frac{k}{d^2}$$

$$I = \frac{P}{A}$$

$$\text{path difference} = m\lambda \quad \text{or} \quad \left(m + \frac{1}{2}\right)\lambda \quad \text{where } m = 0, 1, 2, \dots$$

$$\text{random uncertainty} = \frac{\text{max. value} - \text{min. value}}{\text{number of values}}$$

$$V_{\text{peak}} = \sqrt{2}V_{\text{rms}}$$

$$I_{\text{peak}} = \sqrt{2}I_{\text{rms}}$$

$$Q = It$$

$$V = IR$$

$$P = IV = I^2R = \frac{V^2}{R}$$

$$R_T = R_1 + R_2 + \dots$$

$$\frac{1}{R_T} = \frac{1}{R_1} + \frac{1}{R_2} + \dots$$

$$E = V + Ir$$

$$V_1 = \left( \frac{R_1}{R_1 + R_2} \right) V_s$$

$$\frac{V_1}{V_2} = \frac{R_1}{R_2}$$

$$C = \frac{Q}{V}$$

$$E = \frac{1}{2}QV = \frac{1}{2}CV^2 = \frac{1}{2} \frac{Q^2}{C}$$

# Additional Relationships

## Circle

$$\text{circumference} = 2\pi r$$

$$\text{area} = \pi r^2$$

## Sphere

$$\text{area} = 4\pi r^2$$

$$\text{volume} = \frac{4}{3}\pi r^3$$

## Trigonometry

$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}}$$

$$\sin^2 \theta + \cos^2 \theta = 1$$

## Moment of inertia

point mass

$$I = mr^2$$

rod about centre

$$I = \frac{1}{12}ml^2$$

rod about end

$$I = \frac{1}{3}ml^2$$

disc about centre

$$I = \frac{1}{2}mr^2$$

sphere about centre

$$I = \frac{2}{5}mr^2$$

## Table of standard derivatives

| $f(x)$    | $f'(x)$      |
|-----------|--------------|
| $\sin ax$ | $a \cos ax$  |
| $\cos ax$ | $-a \sin ax$ |

## Table of standard integrals

| $f(x)$    | $\int f(x)dx$              |
|-----------|----------------------------|
| $\sin ax$ | $-\frac{1}{a} \cos ax + C$ |
| $\cos ax$ | $\frac{1}{a} \sin ax + C$  |

### Electron Arrangements of Elements

Group 1    Group 2  
(1)

|                  |                  |                  |           |
|------------------|------------------|------------------|-----------|
| 1                | <b>H</b>         | 4                | <b>Be</b> |
| Hydrogen         | 1                | (2)              |           |
| 3                | <b>Li</b>        | 2,1              | <b>B</b>  |
| Lithium          | 2,1              | 2,2              | Beryllium |
| 11               | <b>Na</b>        | 12               | <b>Mg</b> |
| 2,8,1            | 2,8,1            | 2,8,2            |           |
| Sodium           |                  | Magnessium       |           |
| 19               | <b>K</b>         | 20               | <b>Ca</b> |
| 2,8,8,1          | 2,8,8,1          | 2,8,8,2          | Calcium   |
| Potassium        |                  |                  |           |
| 37               | <b>Rb</b>        | 38               | <b>Sr</b> |
| 2,8,18,8,1       | 2,8,18,8,1       | 2,8,18,8,2       | Strontium |
| Rubidium         |                  |                  |           |
| 55               | <b>Cs</b>        | 56               | <b>Ba</b> |
| 2,8,18,18,8,1    | 2,8,18,18,8,1    | 2,8,18,18,8,2    | Barium    |
| Caesium          |                  |                  |           |
| 87               | <b>Fr</b>        | 88               | <b>Ra</b> |
| 2,8,18,32,18,8,1 | 2,8,18,32,18,8,1 | 2,8,18,32,18,8,2 | Radium    |
| Francium         |                  |                  |           |

### Key

|   |
|---|
| Atomic number<br>Symbol<br>Electron arrangement<br>Name |
|---|

### Transition Elements

|           |                  |               |                   |          |                   |            |                   |            |                   |           |                   |            |                   |              |                   |             |                   |             |                   |
|-----------|------------------|---------------|-------------------|----------|-------------------|------------|-------------------|------------|-------------------|-----------|-------------------|------------|-------------------|--------------|-------------------|-------------|-------------------|-------------|-------------------|
| 21        | <b>Sc</b>        | 22            | <b>Ti</b>         | 23       | <b>V</b>          | 24         | <b>Cr</b>         | 25         | <b>Mn</b>         | 26        | <b>Fe</b>         | 27         | <b>Co</b>         | 28           | <b>Ni</b>         | 29          | <b>Cu</b>         | 30          | <b>Zn</b>         |
| Scandium  | 2,8,9,2          | Titanium      | 2,8,10,2          | Vanadium | 2,8,11,2          | Chromium   | 2,8,13,1          | Manganese  | 2,8,13,2          | Iron      | 2,8,14,2          | Cobalt     | 2,8,15,2          | Nickel       | 2,8,16,2          | Copper      | 2,8,18,1          | Zinc        | 2,8,18,2          |
| (3)       |                  | (4)           |                   | (5)      |                   | (6)        |                   | (7)        |                   | (8)       |                   | (9)        |                   | (10)         |                   | (11)        |                   | (12)        |                   |
| 39        | <b>Y</b>         | 40            | <b>Zr</b>         | 41       | <b>Nb</b>         | 42         | <b>Mo</b>         | 43         | <b>Tc</b>         | 44        | <b>Ru</b>         | 45         | <b>Rh</b>         | 46           | <b>Pd</b>         | 47          | <b>Ag</b>         | 48          | <b>Cd</b>         |
| Yttrium   | 2,8,18,9,2       | Zirconium     | 2,8,18,10,2       | Niobium  | 2,8,18,12,1       | Molybdenum | 2,8,18,13,1       | Technetium | 2,8,18,13,2       | Ruthenium | 2,8,18,15,1       | Rhodium    | 2,8,18,16,1       | Palladium    | 2,8,18,18,0       | Silver      | 2,8,18,18,1       | Cadmium     | 2,8,18,18,2       |
| 57        | <b>La</b>        | 72            | <b>Hf</b>         | 73       | <b>Ta</b>         | 74         | <b>W</b>          | 75         | <b>Re</b>         | 76        | <b>Os</b>         | 77         | <b>Ir</b>         | 78           | <b>Pt</b>         | 79          | <b>Au</b>         | 80          | <b>Hg</b>         |
| Lanthanum | 2,8,18,18,9,2    | Hafnium       | 2,8,18,32,10,2    | Tantalum | 2,8,18,32,11,2    | Tungsten   | 2,8,18,32,12,2    | Rhenium    | 2,8,18,32,13,2    | Osmium    | 2,8,18,32,14,2    | Iridium    | 2,8,18,32,15,2    | Platinum     | 2,8,18,32,17,1    | Gold        | 2,8,18,32,18,1    | Mercury     | 2,8,18,32,18,2    |
| 89        | <b>Ac</b>        | 104           | <b>Rf</b>         | 105      | <b>Db</b>         | 106        | <b>Sg</b>         | 107        | <b>Bh</b>         | 108       | <b>Hs</b>         | 109        | <b>Mt</b>         | 110          | <b>Ds</b>         | 111         | <b>Rg</b>         | 112         | <b>Cn</b>         |
| Actinium  | 2,8,18,32,18,9,2 | Rutherfordium | 2,8,18,32,32,10,2 | Dubnium  | 2,8,18,32,32,11,2 | Seaborgium | 2,8,18,32,32,12,2 | Bohrium    | 2,8,18,32,32,13,2 | Hassium   | 2,8,18,32,32,14,2 | Meitnerium | 2,8,18,32,32,15,2 | Darmstadtium | 2,8,18,32,32,17,1 | Roentgenium | 2,8,18,32,32,18,1 | Copernicium | 2,8,18,32,32,18,2 |

### Lanthanides

|           |               |        |               |              |               |           |               |            |               |          |               |          |               |            |               |         |               |            |               |         |               |        |               |         |               |           |               |          |               |
|-----------|---------------|--------|---------------|--------------|---------------|-----------|---------------|------------|---------------|----------|---------------|----------|---------------|------------|---------------|---------|---------------|------------|---------------|---------|---------------|--------|---------------|---------|---------------|-----------|---------------|----------|---------------|
| 57        | <b>La</b>     | 58     | <b>Ce</b>     | 59           | <b>Pr</b>     | 60        | <b>Nd</b>     | 61         | <b>Pm</b>     | 62       | <b>Sm</b>     | 63       | <b>Eu</b>     | 64         | <b>Gd</b>     | 65      | <b>Tb</b>     | 66         | <b>Dy</b>     | 67      | <b>Ho</b>     | 68     | <b>Er</b>     | 69      | <b>Tm</b>     | 70        | <b>Yb</b>     | 71       | <b>Lu</b>     |
| Lanthanum | 2,8,18,18,9,2 | Cerium | 2,8,18,20,8,2 | Praseodymium | 2,8,18,21,8,2 | Neodymium | 2,8,18,22,8,2 | Promethium | 2,8,18,23,8,2 | Samarium | 2,8,18,24,8,2 | Europium | 2,8,18,25,8,2 | Gadolinium | 2,8,18,25,9,2 | Terbium | 2,8,18,27,8,2 | Dysprosium | 2,8,18,28,8,2 | Holmium | 2,8,18,29,8,2 | Erbium | 2,8,18,30,8,2 | Thulium | 2,8,18,31,8,2 | Ytterbium | 2,8,18,32,8,2 | Lutetium | 2,8,18,32,9,2 |

### Actinides

|          |                  |         |                   |              |                  |         |                  |           |                  |           |                  |           |                  |        |                  |           |                  |             |                  |             |                  |         |                  |             |                  |          |                  |            |                  |
|----------|------------------|---------|-------------------|--------------|------------------|---------|------------------|-----------|------------------|-----------|------------------|-----------|------------------|--------|------------------|-----------|------------------|-------------|------------------|-------------|------------------|---------|------------------|-------------|------------------|----------|------------------|------------|------------------|
| 89       | <b>Ac</b>        | 90      | <b>Th</b>         | 91           | <b>Pa</b>        | 92      | <b>U</b>         | 93        | <b>Np</b>        | 94        | <b>Pu</b>        | 95        | <b>Am</b>        | 96     | <b>Cm</b>        | 97        | <b>Bk</b>        | 98          | <b>Cf</b>        | 99          | <b>Es</b>        | 100     | <b>Fm</b>        | 101         | <b>Md</b>        | 102      | <b>No</b>        | 103        | <b>Lr</b>        |
| Actinium | 2,8,18,32,18,9,2 | Thorium | 2,8,18,32,18,10,2 | Protactinium | 2,8,18,32,20,9,2 | Uranium | 2,8,18,32,21,9,2 | Neptunium | 2,8,18,32,22,9,2 | Plutonium | 2,8,18,32,24,8,2 | Americium | 2,8,18,32,25,8,2 | Curium | 2,8,18,32,25,9,2 | Berkelium | 2,8,18,32,27,8,2 | Californium | 2,8,18,32,28,8,2 | Einsteinium | 2,8,18,32,29,8,2 | Fermium | 2,8,18,32,30,8,2 | Mendelevium | 2,8,18,32,31,8,2 | Nobelium | 2,8,18,32,32,8,2 | Lawrencium | 2,8,18,32,32,9,2 |

Group 3    Group 4    Group 5    Group 6    Group 7    Group 8    Group 9    Group 10  
(18)

|                |           |                |           |                |            |                |           |                |           |                |           |
|----------------|-----------|----------------|-----------|----------------|------------|----------------|-----------|----------------|-----------|----------------|-----------|
| 5              | <b>B</b>  | 6              | <b>C</b>  | 7              | <b>N</b>   | 8              | <b>O</b>  | 9              | <b>F</b>  | 10             | <b>Ne</b> |
| 2,3            | Boron     | 2,4            | Carbon    | 2,5            | Nitrogen   | 2,6            | Oxygen    | 2,7            | Fluorine  | 2,8            | Neon      |
| 13             | <b>Al</b> | 14             | <b>Si</b> | 15             | <b>P</b>   | 16             | <b>S</b>  | 17             | <b>Cl</b> | 18             | <b>Ar</b> |
| 2,8,3          | Aluminium | 2,8,4          | Silicon   | 2,8,5          | Phosphorus | 2,8,6          | Sulfur    | 2,8,7          | Chlorine  | 2,8,8          | Argon     |
| 31             | <b>Ga</b> | 32             | <b>Ge</b> | 33             | <b>As</b>  | 34             | <b>Se</b> | 35             | <b>Br</b> | 36             | <b>Kr</b> |
| 2,8,18,3       | Gallium   | 2,8,18,4       | Germanium | 2,8,18,5       | Arsenic    | 2,8,18,6       | Selenium  | 2,8,18,7       | Bromine   | 2,8,18,8       | Krypton   |
| 49             | <b>In</b> | 50             | <b>Sn</b> | 51             | <b>Sb</b>  | 52             | <b>Te</b> | 53             | <b>I</b>  | 54             | <b>Xe</b> |
| 2,8,18,18,3    | Indium    | 2,8,18,18,4    | Tin       | 2,8,18,18,5    | Antimony   | 2,8,18,18,6    | Tellurium | 2,8,18,18,7    | Iodine    | 2,8,18,18,8    | Xenon     |
| 81             | <b>Tl</b> | 82             | <b>Pb</b> | 83             | <b>Bi</b>  | 84             | <b>Po</b> | 85             | <b>At</b> | 86             | <b>Rn</b> |
| 2,8,18,32,18,3 | Thallium  | 2,8,18,32,18,4 | Lead      | 2,8,18,32,18,5 | Bismuth    | 2,8,18,32,18,6 | Polonium  | 2,8,18,32,18,7 | Astatine  | 2,8,18,32,18,8 | Radon     |

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